

# Flexible Best Generation Mix for Korea Power System Considering CO<sub>2</sub> Constraint – Vision 2030

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**Abstract --** This paper proposes a fuzzy linear programming based solution approach for the long-term generation mix with multi-stages (years) considering air pollution constraints on CO<sub>2</sub> emissions, under uncertain circumstances as like as ambiguities of budget and reliability criterion level. This paper approaches to generation mix problem for 2030 year in Korea eventually. The proposed approach may give more flexible solution rather than too robust plan. The effectiveness of the proposed approach is demonstrated by applying it to solve the multi-years best generation mix problem on the Korea power system which contains nuclear, coal, LNG, oil and pumped-storage hydro plants.

**Index Terms —** fuzzy linear programming, best generation mix, air pollution

## I. INTRODUCTION

There is a global trend towards liberalization and privatization of the electricity supply industry. This is coupled with growing environmental awareness and increasing prospects ratification of the Kyoto Protocol.[1] Electricity is the indispensable form of energy in modern societies. In this paper, a new approach for the long-term generation mix with multi-criteria considering air pollution constraints, which are not only SO<sub>2</sub> and NO<sub>x</sub> but also CO<sub>2</sub> emission limitations, under the uncertain circumstances is proposed using linear programming. The effectiveness of the proposed approach is demonstrated by applying to the best generation mix problem of Korea power system, which contains nuclear, coal, LNG, oil and pumped-storage hydro plant in multi-years. This case study in this paper is mainly focused on CO<sub>2</sub> emission limitation effect in the best generation mix. The method can accommodate the operation of the pumped-storage generator which has a relationship with operation of nuclear power plant with some strict for load following.[2-7]

This paper approaches to flexible generation mix problem for 2030 year in Korea eventually, which is called vision 2030.

The proposed approach may give more flexible solution rather than too robust plan.

## II. THE CONCEPT OF FLEXIBLE PLANNING

In recently, the uncertainties of external conditions for power system scheduling problem, demand growth, primary energy resource circumstances, reliability of energy supply system and energy security are becoming more and more unmanageable. The uncertainties require more flexible system for preventing power system from the unmanageable collapse. Fig.1 means that the flexible planning and operation for power system is one which,

“Although not necessarily gives the optimum solution for the basic forecasted conditions, yet can keep the reasonable scheduling solution from being significantly worsened by any assumed changes in the surrounding situations” [8,9].

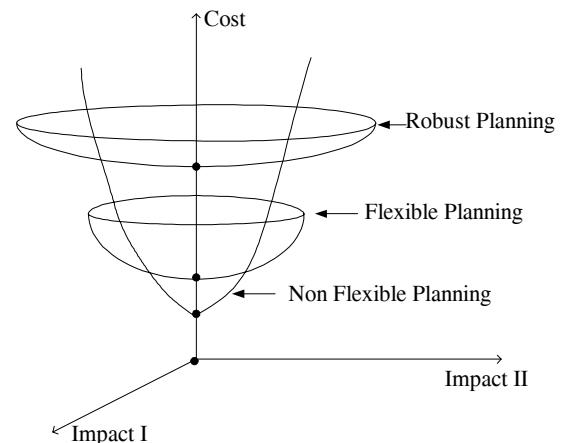


Fig. 1. Concept of flexibility

The useful methods for flexible generators mix problem and generators maintenance flexible scheduling problem using fuzzy LP, DP, IP and search method have been developed by the authors [3-23]. Some cases of application of fuzzy set theory for the flexible planning and operation of power systems are introduced in this seminar. It is expected that more flexible solution can be obtained with the proposed methods because the fuzzy set theory that can reflect the subjective decision of decision-maker is used in these studies. This paper uses fuzzy set theory in order to get a flexible long-term generation mix solution in Korea power system considering CO<sub>2</sub> emission constraint.

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### III. THE LP FORMULATION OF BEST GENERATION MIX

#### A. Problem statement

This problem can be defined as to determine the generation mix under the following assumptions:

- (1) The annual loads are given.
  - (2) The number of generator is not that of units but that of types.
  - (3) Nuclear power plants are able to perform load following.
- The system for the proposed method can be modeled as shown in Fig. 2.

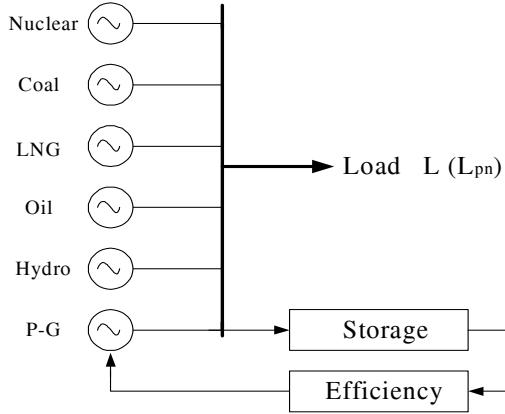


Fig. 2. A system model for the proposed method

In this study, it is assumed that the hydro generator construction is separately planned from that of the other kinds of generation units. In actual system, the basic resources, which are reserves, of the hydro power plants have limitation in the country. Therefore, the choice of hydro plant construction is not much and non-flexible. Under the assumption, the best generation mix problem is formulated as followings.

#### B. Objective functions

##### The economic criterion:

The economic criterion in the best generation mix is minimization of the sum of the construction cost and the fuel cost as

$$\text{Minimize } Z = \sum_{n=1}^{N_{NG}} \sum_{i=1}^{NG} K_{cin} d_{in} \alpha_i \Delta x_{in} + \sum_{n=1}^{N_{NG}} \sum_{i=1}^{NG} K_{fin} f_{in} y_{in}$$

$$= F(\Delta x_{in}, y_{in})$$

where,  $i$ : unit type number (1 for nuclear, 2 for coal, 3 for LNG, 4 for oil, and 5 for pumped-storage generators are specified in this paper)

$N$ : number of total study stage year

$NG$ : number of unit type

$$K_{cin} = ((1+e_{ci})/(1+r))^{n_{Tn}}$$

$$K_{fin} = ((1+e_{fi})/(1+r))^{n_{Tn}}$$

$e_{ci}$ : apparent escalation rate of construction materials of  $i$ -unit

$e_{fi}$ : apparent escalation rate of fuel of  $i$ -unit

$r$ : discount rate

$\Delta T_{k,k-1}$ : step size years of study years from  $k$  to  $k-1$

$d_{in}$ : construction cost of the  $i$ -unit in  $n$  year

$f_{in}$ : marginal fuel cost of the  $i$ -unit in  $n$  year [Won/MWh]

$\alpha_i$ : annual expenses rate of the  $i$ -unit

$\Delta x_{in}$ : construction capacity of the  $i$ -unit in  $n$  year [MW]

$y_{in}$ : generation capacity of the  $i$ -unit in  $n$  year [MWh]

#### C. Constraints

##### 1) Installed capacity constraint

$$\sum_{i=1}^{NG} (x_{in-1} + \Delta x_{in}) + HYD_n \geq L_{pn} (1+R_n) \quad n=1 \sim N$$

where,  $R_n$ : supply reserve rate in  $n$  year. [p.u]

$HYD_n$ : capacity of hydro generator in  $n$  year. It is assumed that the  $HYD_n$  is given in this study.

##### 2) Energy constraint of demand

$$\sum_{i=1}^{NG} y_{in} \geq (L_{pn} + L_{Bn}) \times 8760/2 + V_n - HYD_n \times 8760 \times CF_H$$

where,  $L_{pn}$ : peak load at  $n$  year

$L_{Bn}$ : base load at  $n$  year

$V_n$ : the added demand energy is caused by pumped-storage generator

$CF_H$ : average capacity factor of hydro generator

##### 3) Production energy constraint of generation system

$$y_{in} \leq (x_{in-1} + \Delta x_{in}) \times 8760 \times CF_i \quad i=1 \sim NG, \quad n=1 \sim N$$

where,  $CF_i$ : average capacity factor of the  $i$ -unit

##### 4) Capacity constraint in initial year

$$x_{i0} = EX_i \quad i=1 \sim NG$$

where,  $EX_i$ : capacity of the  $i$ -existing unit

##### 5) Constraint of mutual relationship between existing generator capacity and new generator capacity (state equation)

$$x_{in} = x_{in-1} + \Delta x_{in} \quad i=1 \sim NG, \quad n=1 \sim N$$

##### 6) Energy constraint of LNG thermal plant

$$y_{3n} \geq LEP_{min}/\rho_3 \quad n=1 \sim N$$

where,  $LEP_{min,n}$ : LNG thermal generator production energy for LNG minimum due to consumption in  $n$  year

##### 7) Constraints of reservoir capacity of pumped-storage generator

$$y_{5n} = \eta_g \times Vn$$

where,  $\eta_g$ : efficiency of pumped-storage generator

##### 8) No load following power constraints of nuclear power plant

$$(x_{In} - x_{5n}) \leq L_{Bn} \quad n=1 \sim N$$

### 9) Upper-lower constraints of new unit capacity

$$\Delta x_{in} \leq \Delta X_{max\ in} \quad i=1 \sim NG, n=1 \sim N$$

where,  $X_{min\ in}$  and  $X_{max\ in}$  are minimum and maximum capacity of new unit at  $n$  years(period) respectively.

### 10) $CO_2$ air pollution constraint

$$\sum_{i=1}^{NG} \xi_i y_i \leq CO_{2MAXn}$$

where,  $CO_{2MAXn}$ : maximum quantity of  $CO_2$  permitted in  $n$  year  
[Ton/yr]

$\xi_i$ : fuel consumption rate of the  $i$ - unit [Ton/MWh]

### 11) $SO_x$ air pollution constraint

$$\sum_{i=1}^{NG} SO_{Xin} \xi_i y_n \leq SO_{XMAXn}$$

where,  $SO_{Xin}$ :  $SO_x$  density of the  $i$ - unit in  $n$  year [ppm/Ton]

$SO_{XMAXn}$ : maximum quantity of  $SO_x$  permitted in  $n$  year  
[Ton/yr]

### 12) $NO_x$ air pollution constrain

$$\sum_{i=1}^{NG} NO_{Xin} \xi_i y_n \leq NO_{XMAXn}$$

where,  $NO_{Xin}$ :  $NO_x$  density of the  $i$ - unit in  $n$  year [ppm/Ton]

$NO_{XMAXn}$ : maximum quantity of  $NO_x$  permitted in  $n$  year  
[Ton/yr]

## IV. THE FUZZY LP FORMULATION OF FLEXIBLE GENERATION MIX

### A. The Optimal Decision Theory by Fuzzy Set Theory

The fuzzy decision  $D$  resulting from  $q$  fuzzy goals  $G_1, \dots, G_q$  and  $p$  fuzzy constraints  $C_1, \dots, C_p$  is the intersection of them;

$$D = (\bigcap_{i=1}^q G_i) \cap (\bigcap_{j=1}^p C_j) \quad (1)$$

and also its membership function  $\mu_D$  resulting from fuzzy goals and constraints is defined by

$$\mu_D(\mathbf{x}) = \min_{i=1 \sim p} [\min_{j=1 \sim q} \mu_{Gj}, \min_{j=1 \sim q} \mu_{Cj}] \quad (2)$$

Where, min is an abbreviation of minimum. The fuzzy mathematical programming problem consists of finding the maximum of the fuzzy decision  $D$ .

$$\mu_D(\mathbf{x}^*) = \max \mu_D(\mathbf{x}) \quad (3)$$

where  $\mathbf{x}^*$  is the optimal decision solution max is an abbreviation of maximum. The vector eq.(3) can be rewritten as the eq.(4) .

$$\mu_D(x_1^*, x_2^*, \dots, x_N^*) = \max_{x_1 \dots x_N} \mu_D(x_1, x_2, \dots, x_N) \quad (4)$$

Fig. 3 shows the concept for optimal decision on fuzzy sets, which is proposed by Bellman Zadeh[6].

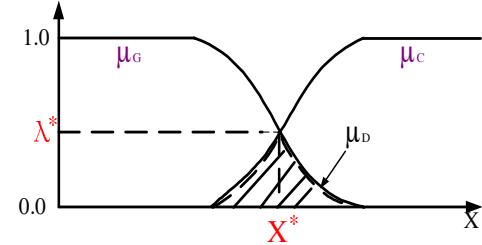


Fig. 3. Concept for optimal decision on fuzzy sets

### B. The function of Fuzzy linear programming

#### Fuzziness of Cost : $Z \leq Z_0$

The Satisfaction Level in the best generation mix is flexible because the total cost is unjustly.

#### Fuzziness of Reliability criterion : $R_n \geq R_{0n}$

The reliability criterion in the long term based best generation mix may be flexible criterion than entirely strict.

Using parameter  $\lambda$ , therefore, which means satisfaction level physically, best generation mix problem can be formulated as following.

#### Objective functions: Maximize $\lambda$

#### Constraints : Subject to $F(\Delta x_{in}, y_{in}) + \Delta Z_0 \lambda = Z_0 + \Delta Z_0$

$$(\sum_{i=1}^{NG} (x_{in-1} + \Delta x_{in}) + HYD_n - L_{Pn}) / L_{Pn} - \Delta R_0 \lambda = R_0 - \Delta R_0$$

$$\sum_{i=1}^{NG} y_{in} \geq (L_{Pn} + L_{Bn}) \times 8760/2 + V_n - HYD_n \times 8760 \times CF_H$$

$$y_{in} \leq (x_{in-1} + \Delta x_{in}) \times 8760 \times CF_i$$

$$x_{i0} = EX_i$$

$$x_{in} = x_{in-1} + \Delta x_{in}$$

$$y_{3n} \geq LEP_{min} / \rho_3$$

$$y_{5n} = \eta_g \times V_n$$

$$(x_{In} - x_{5n}) \leq L_{Bn}$$

$$\Delta x_{in} \leq \Delta X_{max\ in}$$

$$\sum_{i=1}^{NG} \xi_i y_i \leq CO_{2MAXn}$$

$$\sum_{i=1}^{NG} SO_{Xin} \xi_i y_n \leq SO_{XMAXn}$$

$$\sum_{i=1}^{NG} NO_{Xin} \xi_i y_n \leq NO_{XMAXn}$$

## V. CASE STUDIES

In order to demonstrate the effectiveness of the proposed method the generation mix is performed on Korea power system, which consists of 6 types generators over 25 years (2006-2030). It is assumed that the initial year is 2006. The step size of planning year is assumed as five years ( $\Delta T=5$ ). The maximum, minimum load and hydro capacity in standard years are listed in table I. The characteristics and economic data are summarized in table II and table III, respectively. [11]

TABLE I

MAXIMUM LOAD, MINIMUM LOAD, AND HYDRO PLANT AT STANDARD YEARS

Years	Peak load $L_P$ [MW]	Base load $L_B$ [MW]	Hydro [MW]	LEP ( $10^3$ Ton)
2006	58,990	35,394	1,800	--
2011	65,940	39,564	2,000	4,500
2016	70,050	42,030	2,200	5,500
2021	74,000	44,400	2,400	6,500
2026	77,000	46,200	2,600	7,500
2030	80,000	48,000	2,600	7,500

TABLE II

MAXIMUM LOAD, MINIMUM LOAD, AND HYDRO PLANT AT STANDARD YEARS

Gen. Type	Initial capacity [MW]	Fixed charge [ $10^5$ won/kW]	$A_{ER}$ of fixed charge [%]	Marginal fuel cost [Won/kW]	$A_{ER}$ of fuel cost [%]
Nucl.	17,716	144.4	3.5	4	1
Coal	18,465	79.7	3.4	17	1
LNG	17,437	61.4	3.3	67	1
Oil	4,686	153.2	3.3	87	4
P-G	3,300	63.4	3.5	0	0

Annual cost rate [%]	Capacity factor [%]	Fuel consumption rate [Ton/MWh]	Density [ppm/Ton] $CO_2$ , $SO_2$ , $NO_x$
19	90	--	
17	90	0.2300	700 450 500
17	60	0.1100	450 200 300
17	55	0.2000	600 200 100
13	30	--	

(where:  $A_{ER}$  means the apparent escalation rate and the discount rate is assumed as 7.5%)

Maximum new construction capacity is limited by limitation of human and equipment resources, etc. It is assumed, as shown in Table III, that the maximum and minimum capacities per a stage year of new generator are same for all stage/year in this study.

TABLE III

MAXIMUM AND MINIMUM OF CAPACITY PER A STAGE YEAR OF NEW GENERATORS ([MW])

Gen. Type	$\Delta X_{max}$	$X_{max}$
Nuclear	5,000	30,000
Coal	5,000	30,000
LNG	5,000	30,000
Oil	500	2,500
P-G	1,000	5,000

TABLE IV

MAXIMUM PERMISSIBLE LIMITATION OF AIR POLLUTION EMISSION ( $10^3$  [TON/YR])

Air pollution	2011	2016	2021	2026	2030
$CO_2$	40	40	40	40	40
$SO_2$	40	40	40	40	40
$NO_x$	40	40	40	40	40

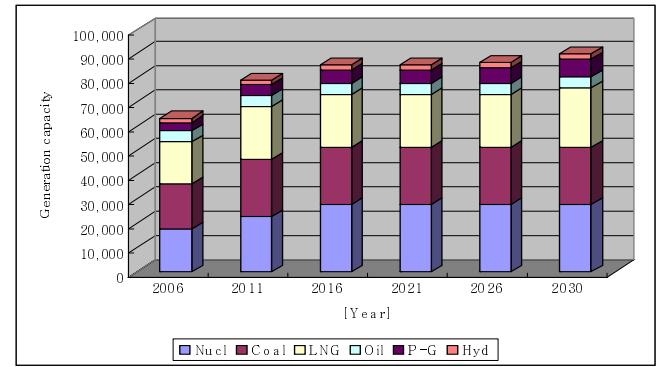
### A. Results by Non-Fuzzy model

The simulated results in the cases; base case not considering air pollution criterion and case1 considering air pollution criterion, are shown in Table V and Table VI. The proposed fuzzy set theory based on best generation mixes, which are simulated under considering air pollution criterion are different from the generation mix using conventional method. The results yield that the mix of nuclear power plants is increasing and that of coal power plants is decreasing. Fig. 4 and Fig. 5 shows total capacity and percent ratio results for conventional method and proposed method considering air pollution constraints.

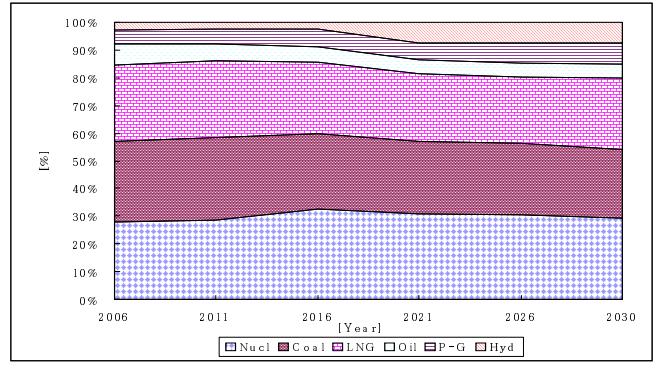
TABLE V

BEST GENERATION MIX FOR THE CONVENTIONAL METHODS. [%]

Gen. type	Conventional method (Base Case: Case 0)					
	2006	2011	2016	2021	2026	2030
Nucl.	27.94	28.71	32.48	35.51	35.05	33.74
Coal	29.12	29.65	27.50	25.73	25.40	24.44
LNG	27.50	27.75	25.74	24.08	23.77	25.58
Oil	7.39	5.92	5.49	5.14	5.07	4.88
P-G	5.20	5.43	6.21	6.91	7.90	8.65
Hyd	28.4	2.53	2.58	2.63	2.81	2.71



(a) Total capacity



(b) Percent ratio

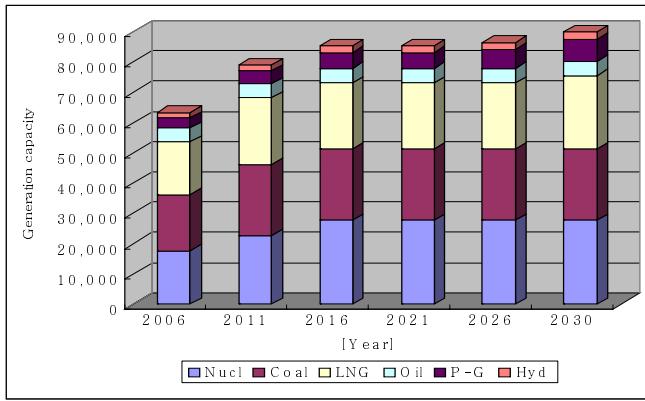
Fig. 4. Best generation mix by Conventional method (case 0)

Table VII and Fig. 6 show the results of sensitivity analysis of permissible maximum for CO<sub>2</sub> constraint. As the air pollution constraints are considered, the mix of nuclear power plant is growing up and the total cost is increasing.

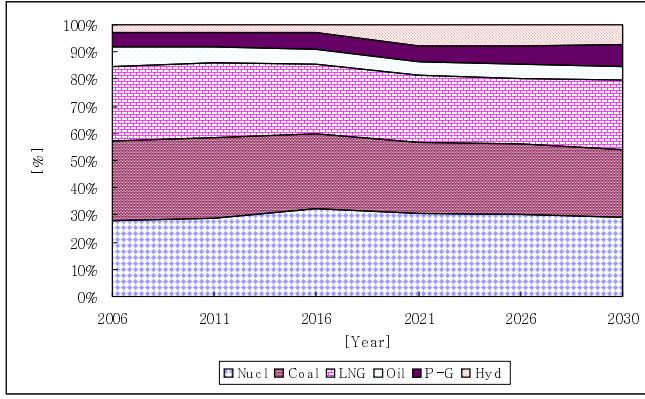
TABLE VI  
BEST GENERATION MIX FOR THE PROPOSED METHODS. [%]

Gen. type	Proposed method - APC reinforcement mix (Case 1)					
	2006	2011	2016	2021	2026	2030
Nucl	27.94	28.71	32.47	35.62	35.16	33.91
Coal	29.12	29.65	27.53	25.71	25.38	24.48
LNG	27.50	27.75	25.73	24.03	23.71	25.37
Oil	7.39	5.92	5.49	5.13	5.06	4.88
P-G	5.20	5.43	6.21	6.89	7.88	8.65
Hyd	28.4	2.53	2.58	2.63	2.81	2.71

(where, APC means the air pollution(CO<sub>2</sub>, SO<sub>2</sub> and NO<sub>x</sub>) constraints)



(a) Total capacity



(b) Percent ratio

Fig. 5. Best generation mix by proposed method with CO<sub>2</sub> air pollution constraint (case 1)

### B. Results in Fuzzy model

The proposed fuzzy set theory based best generation mixes which are simulated under considering air pollution criterion are different from the generation mix using conventional method. The results are shown in Table VIII. Where, satisfaction level ( $Z_0$ ) is  $16.5 \times 10^3$ [billion won] and  $\Delta Z_0$  is 10[%] of  $Z_0$ . Table IX shows the comparison of costs and satisfaction levels of best generation mix in three cases.

TABLE VII  
COST VARIATION ACCORDING TO CHANGING OF THE CO<sub>2</sub> GAS AIR POLLUTION CONSTRAINTS. [BILLION WON]

	Permissible maximum For CO <sub>2</sub> constraint x 10 <sup>6</sup> [Ton/yr]	Construction Cost	Operating Cost	Total Cost
Case 0	-	4,475.10	11,238.99	15,714.09
Case 1	40	4,498.82	12,018.50	16,517.32
Case 2	35	4,531.21	12,468.79	17,000.00
Case 3	30	4,563.62	12,919.07	17,482.69
Case 4	25	4,596.02	13,369.35	17,965.37
Case 5	20	4,638.19	13,826.55	18,464.74

[Billion won]

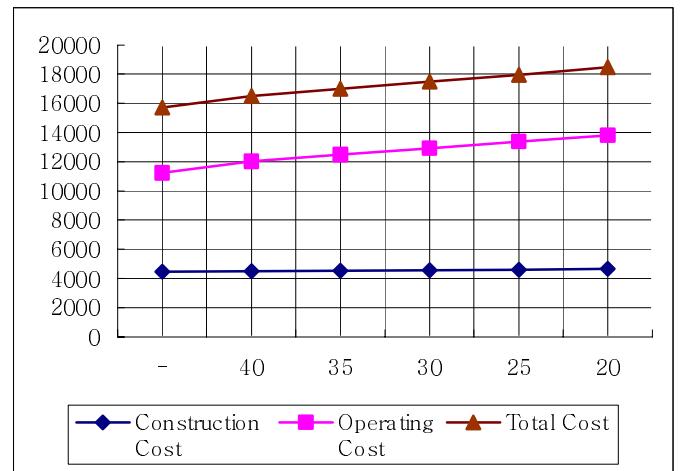


Fig. 6. Construction, fuel and total costs variation according to gas emission constraints.

TABLE VIII  
BEST GENERATION MIX FOR APC REINFORCEMENT MIX USING FUZZY SET THEORY [%]

Gen. type	Proposed method - APC reinforcement mix					
	2006	2011	2016	2021	2026	2030
Nucl	27.94	28.71	32.47	35.62	35.16	33.91
Coal	29.12	29.65	27.53	25.71	25.38	24.48
LNG	27.50	27.75	25.73	24.03	23.71	25.37
Oil	7.39	5.92	5.49	5.13	5.06	4.88
P-G	5.20	5.43	6.21	6.89	7.88	8.65
Hyd	28.4	2.53	2.58	2.63	2.81	2.71

TABLE IX  
TOTAL COST EVALUATION OF BEST GENERATION MIX IN THE THREE CASES.  
[Billion Won]

	Construction Cost	Operation Cost	Total Cost	Satisfaction Level
Conventional method (Case 1)	4,498.82	12,018.50	16,517.32	-
Mix without APC (Case FA1)	4,475.10	11,238.99	15,714.09	0.98
Mix with APC (Case FB4)	4,498.82	12,018.50	16,517.32	0.49

Table X and Fig 7 show the relationship between  $Z_0$  and satisfaction level for various aspiration targets using fuzzy set theory. As satisfaction level of 0.1 point increases, the total cost increases about 150 billion [Won]. Where, the abbreviation, APC means air pollution constraint of  $\text{CO}_2$ ,  $\text{SO}_x$  and  $\text{NO}_x$ . The result recommends informs about the incremental rate value of cost in order to make one unit of satisfaction level higher.

TABLE X  
SATISFACTION LEVEL VARIATION ACCORDING TO CHANGING OF COST ASPIRATION LEVEL

	Cases	Aspiration level $z_0$ [ $10^3$ Billion won]	Satisfaction level $\lambda$
APC not considered Cases	Fuzzy A1	16.5	0.98
	Fuzzy A2	16.4	0.92
	Fuzzy A3	16.3	0.86
	Fuzzy A4	16.2	0.80
APC considered Cases	Fuzzy B1	17.4	1.00
	Fuzzy B2	17.1	0.84
	Fuzzy B3	16.8	0.67
	Fuzzy B4	16.5	0.49

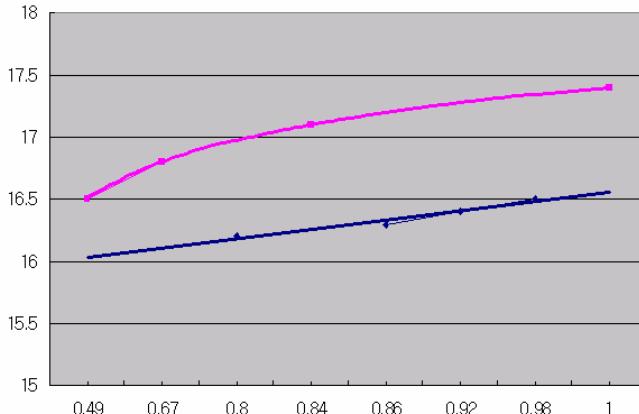


Fig. 7 Satisfaction level variation according to changing of cost aspiration level

## VI. CONCLUSIONS

In this paper, an alternative approach for the long-term generation mix with multi-criteria considering air pollution constraints, which are not only  $\text{SO}_2$  and  $\text{NO}_x$  but also  $\text{CO}_2$  emission limitations is proposed using linear programming. The effectiveness of the proposed approach is demonstrated by applying to the best generation mix problem of Korea power system, which contains nuclear, coal, LNG, oil and pumped-storage hydro plant in multi-years. This paper approaches to generation mix problem for 2030 year in Korea eventually. The result is nuclear 33.9[%], coal 24.5[%], LNG 25.4[%], and pumped-storage generator 8.7[%]. The method can accommodate the operation of the pumped-storage generator which has a relationship with operation of nuclear power plant with some strict for load following. This case study in this paper is mainly focused on  $\text{CO}_2$  emission limitation effect in the best generation mix. The  $\text{CO}_2$  air pollution constraint is more strict, the nuclear or LNG power plant construction is recommended as shown in the case study

although the total cost is increasing. So the increasing cost is called the cost for air pollution constraints. The cost for air pollution constraints is [0.82Won/kWh]. Although it is just an example, it is will basic date of carbon dioxide emission trading market. From sensitivity analysis between satisfaction level and cost, decision makers can obtain informs of the incremental rate value of cost in order to make one unit of satisfaction level higher.

## VII. ACKNOWLEDGMENT

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